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Graphing Henderson Creek: A Case of Relations in Sociomaterial Practice

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Introduction

Over the past decade, it has almost become a truism to say that the mathematics in school and the mathematics in everyday settings are considerably different, and often incommensurable. However, it is much less evident what the competencies are people bring to (implicit or explicit) mathematical tasks in everyday situations. In the following episode, Nadine, a beginning mathematics and science teacher visits a farm that is part of a movement in the valley to improve the health of a local creek and watershed. (Pseudonyms replace proper names throughout this chapter.) She meets with Karen, a water technician working on the farm and paid to a considerable part by a grant from a governmental agency. Karen is also part of an environmentalist movement that has taken as its goal to improve the watershed and to design the creek, its riparian zones, and the practices of the people living in it (see Lee & Roth, 1999).

One of the first things Karen shows Nadine is the water monitoring station, which essentially consists of a pen chart recorder that continuously inscribes water levels on a paper roll. In the following excerpt, Karen reads the graph and provides some explanations. In the process, she points and moves along the graph using deictic and iconic gestures (Figure 1).

01 K: So, this [b] is a 24 hour time period, so time's going this way on the

variations within and across seasons (see also Figure 5.c). In contrast to the 11 and 27 liter/second volumes that are, in Karen's descriptive language, "low" and "quite high," we get a sense of the variability of summer flows. Furthermore, Karen's understanding does not stop with the numerical values of the volumes. She knows about fish and the conditions they need (lines 12-14). She is familiar with the temperatures that go with different water levels and, in turn, influence the conditions of the water as habitat. For Karen, all of this is part of what constitutes her competent reading.

The fish Karen talks about are not abstract objects somewhere out there. Rather, they are intimately related to her activities in her watershed-related world. She participates in capturing the trout in traps for measurement purposes, counts them making use of an electroshock device, and brings them to the surface by throwing small spitball-sized chewed paper into the pools. She knows that they prefer the areas below the riffles that she builds, where the water has a higher dissolved-oxygen (DO) content as indicated by her DO meter. She is familiar with the accounts given by elders from the nearby First Nations village. They still talk about the 18-inch cutthroat that they used to fish in the creek. Karen has read the notebook entries of the local priest who was able to capture a dozen trout in the course of one morning. That is, there is more to Karen's explanation than the graph as such. The object of her knowing is first and foremost the creek, knowledge *of* the creek, while the graph is *one* of the tools mediating her knowledge *about* the creek. Her talk is about the summer and about fish that need a certain amount of water. I argue that Karen's reading of the graph, in fact her competency, derives from a dense network of activities, practices, and facts. It is this dense network to other graphs, instruments, and practices that situates Karen's competency and allows these graph-related competencies to exist in the first place.

The excerpt also already shows two other aspects. First, without the gestures, it is virtually unknowable what the referent of Karen's talk is. So as a first step, we include these as part of our analysis. Furthermore, Karen's gestures and talk do not stand on their own but are over and about the graph. They are about the graph, that is, the graph is the topic of Karen's talk. But

importantly, the talk is also over the graph in the sense that the latter serves as indexical ground. I argue that it makes sense to use a cognitive unit of analysis that includes the entire performance, talk and gesture, and the graph. Second, graph reading exists in a social nexus. Here, Nadine constitutes herself and is constituted as a listener. Karen talks about her work and how the graph inscribes itself in the practices. But she does not just narrate irrespective of the listener. Nadine signals that she is still with the narrative at those points where breaks in the narration allow her to take a turn (lines 07, 11). This pattern is changed only once when Nadine expresses amazement about the extreme low levels of water during the summer months.

In the past, much research on mathematical knowing has focused on models of mind irrespective of context. This approach is being questioned, for it neglects the contexts that enable cognition to exist in the first place. Here, context is viewed as the historically constituted concrete relations within and between situations (e.g., Lave, 1988; Walkerdine, 1988). I take the view that knowledge is not an entity that can be acquired but rather that knowing is equivalent to acting in the world; knowing is a process rather than a state. Knowing arises from historically constituted (concrete) relations within and between sociomaterial¹ situations and involves the individual body as much as the individual mind. The body-mind ensemble is an indissociable sociomaterial entity subject to be formed by the sociomaterial world to which it is connected and that embeds it. I am therefore interested in the position that “the relational dynamics [between sign and practice] are not created inter-subjectively in any simple sense, but are produced in relation to aspects of social practice which are culturally and historically specific” (Walkerdine, 1988, p. 12)

I begin by contextualizing my work in two ways. First, because graphs have sign functions, I provide a brief overview of a semiotic approach to graphing. Second, as the introductory analysis of Karen’s work shows, graphs are embedded in numerous other relations requiring an expanded framework. I present one such framework derived from activity theory. After a brief exposition

¹ I choose to link the social and material rather than the social and historical, or the social and the cultural because I view all social practices as historically contingent and embedded in some culture. However, the material aspects of cognition are seldom enough emphasized or, as in traditional cognitive science completely left out of the modeling of knowing and learning.

of the way, we encounter elementary forms of mathematical practices that always involve the physical body of the researcher. The gap seemingly disappears in the practices of the scientists who enact continuous series of transformations. This research aligns itself with semiotics, a line of research concerned with the relation between signs and things in the world relatively little consulted by mathematics educators.

For nearly one hundred years, semioticians (e.g., Peirce, Saussure, and Eco) have researched the relationship between world and language, signs and their referents (Nöth, 1990). They recognized that there existed an ontological gap between signs and their referents. Those following the path of Charles Sanders Peirce propose that while we cannot close the gap, we can always superpose another, sign-sign relation on top of the first relation (e.g., Ricœur, 1991). This second relation between a sign and another sign, its interpretant, elaborates the first relation, which remains inaccessible in principle (Figure 2b). For example, the sign /dog/ refers to some aspect of the world. The relation between the sign /dog/ and the class of entity, «dog», that it refers to can be elaborated by other signs such as a drawing, the equivalent in another language (e.g., chien [French], Hund [German]), a metaphoric use such as /fidelity/, and so forth. Here, each production of an interpretant sign constitutes a translation of the original sign. The process of translation (interpretation) is unlimited, because there are many, potentially an infinite number of interpretant signs (Figure 2b). Semioticians refer to this process as unlimited semiosis (e.g., Eco, 1984).

When we follow scientists (or any other individual involved in sign production), we begin to notice a series of (potentially infinite) translations. These translations turn, for example, living lizards caught somewhere in the mountains of the Pacific Northwest into a statement such as “there is a significant correlation between lizard sprint speed and leg length.” This statement itself translates and is translated by a graph or statistical information (e.g., p , r , R^2). (For a detailed ethnographic study of such activities see Roth & Bowen, 1999b.) For example, a two-column table of numbers and a Cartesian graph are equivalent because of established practices, not because there is an inherent logical connection between the two. Similarly, a mathematical

function such as $f[x] = x^2 - 3$ and a parabolic curve on a Cartesian graph are equivalent because of established and shared mathematical practices, not because of some internal logical relation.

Following scientists around we come to see chains of elements, each of which plays the role of sign for the previous element and the role of thing/ matter for the previous giving rise to a chain of signification (Figure 2c). That is, each element constitutes a map for the previous element, its territory; in turn, it becomes territory for the subsequent element. It is important to note, however, the consecutive elements are separated by an ontological gap. The links across each gap are established as a matter of social practices, which are shared within and constitutive of particular communities. This view is commensurable with semiotic processes operating at multiple hierarchical scales in which elements to the right in Figure 2c are the objects of an element in the middle, which themselves are signs in a system of interpretants (Lemke, in press). The semiotic processes relating to the lines of graphs themselves are inscribed in topological semiotics, whereas entities such as the variables (axes labels) inscribe themselves in typological semiotics (Lemke, 1999).

Graphing and Activity Systems

Traditionally, sign-reference relationship was the primary object of research in mathematical cognition. More recently, it has been recognized that this relationship is not independent of the community of interpreters, which led us to a semiotic approach (and, equivalently, to the theory of community of practice [Lave & Wenger, 1991]). But even considering the community of interpreters is insufficient to account for mathematical understanding; that is, a semiotic analysis is therefore only part of the story. To capture the other parts, I draw on activity theory (e.g., Engeström, 1993). My introductory description and analysis of Karen in activity brought out a number of relations. Thus, Karen focuses on the creek that her farm needs as a water supply throughout the season, but this relation is mediated by the graph. Both the creek and the graph are historically and culturally situated. First Nations and other people have been drawing water from the creek for hundreds of years, and Western farmers have received licenses since the 1940s. The graph as the product of a pen chart recorder is embedded in scientific and

In the present study, I show that Karen's reading of the graph in terms of the water levels of Henderson Creek is inscribed in many other relations, some of which are made thematic in Figure 3. For example, the primary relation of subject (Karen), object (Henderson Creek), and mediating artifact (graph) is mediated by another which exists between herself, the community (here represented by the Mayor Walter) and the graph. Yet another relation made thematic in this chapter is that between the Mayor Walter, the Henderson Creek watershed, and Karen. Still another mediated relation is that between Karen, the water levels, and the Environment Canada technician who comes to establish the calibration curve that allows Karen to read her graph in terms of liters/second although it really displays water levels. In another triangle, the graph replaces Henderson Creek as the object and is, in turn, mediated by other graphs.

Graphs provide the basis whereby particular physical relations are inscribed as relations within the organization of practice. In such cases, we cannot speak simply of "representation" because signs represent more than physical relations (Walkerline, 1988). As beings, we always come to a world where graphs, as signs in general, are always and already social (Heidegger, 1977). In Karen's work, the graph taps many other practices (signifying and material) within the valley, irrigation, damming the creek, fishing, habitat maintenance, building impervious surfaces, building riffles, planting trees in riparian zones, oxygenating the creek. It is in relation to these other practices that Karen's graphing exists. Looking at her graph reading in the absence of everything else, we could come to the conclusion that she competently reads it. But this is of little help for understanding the relations that make this graphing competence possible in the first place.

Background of the Study

The data presented in this chapter derive from a large three-year study on the representation practices among scientists (almost exclusively ecologists) and environmental activists.³ This study included both formal interview situations in which participants were asked to read and

³ My former graduate students Michelle McGinn and Michael Bowen participated in this large-scale study of scientific representation practices.

elaborate on graphs that we had culled from introductory university ecology courses and textbooks. We also conducted multi-year ethnographies in field research settings and in an environmental activist group that focused its activities on the Henderson Creek watershed and the community of Oceanside. One of these activists was Karen, a water technician employed by a local farmer with funds from a government grant. The farmer had environmental concerns related to the water resources in the Henderson Creek watershed where his farm is located, and especially in regards to the creek from which he obtains the water for irrigating his fields. Among others, Karen operated a device that continuously monitors the water level in the creek by means of a pen chart recorder.

In addition to the research among the environmental activists, we also designed and enacted a science curriculum in which elementary children have opportunities to engage in (mostly mathematical) representation practices. The children constructed representations about the creek and its environs with the ultimate goal of feeding their understandings back into the community during an open house organized annually by the activists. As part of this work, Karen and the activists worked with teachers, such as Nadine, to familiarize them with her work on the farm and among the activists.

The materials used in this chapter derive from four videotaped situations where Karen explained the water level graphs and talked about the graphs with teachers and visitors at the open house. In addition, I spent considerable time with Karen walking in and alongside the creek, studying the habitats from the mouth of the creek to its beginnings. We spent time talking about the watershed while standing far above the creek, or walking the fields of the farm. Furthermore, we spent considerable time together working with grade 7 students in the creek, teaching them how to collect data, make observations, and how to understand the watershed as an ecosystem. Our conversations were recorded in the form of videotapes, audiotapes, and fieldnotes. Some materials on which I draw derive from grant proposals written by the activists to garner funds for their activities. I further draw on understandings deriving from our

ethnographic work among the activists. (A detailed study of the representation practices was presented at a recent social studies of science conference [Lee & Roth, 1999].)

Knowing Graphing: Relations in Praxis

In this section, I describe some of the relations within my unit of analysis. My primary focus is Karen, the subject at the base of the mediating triangle (Figure 3). My research on graphing suggests that relations such as those described here are fundamental to the constitution of competence. A detailed analysis showed that Karen was highly competent and each feature of the water level graphs provided her with a window into her world, the Henderson Creek watershed (Roth & Bowen, in press). Here, I do not want to return to that analysis but rather provide evidence for the different kinds of relations that go with the knowledge that we had documented earlier.

Historical Context of Henderson Creek and Oceanside

Karen and the graph she reads to the visitors on the farm and Open House do not exist in a vacuum. Rather, Henderson Creek and the community located within its watershed boundaries have their own political, social, and economic histories. Commuting into the community and working with the people that inhabit the watershed provides Karen with many opportunities to find out about past events and the historical evolution of water-related contexts. Thus, although she had been around for only four years, and although the water level monitoring station has existed for about the same time, she can make then-and-now comparisons of the amount of water coming through the creek after a specific rainfall event. (The positioning of Karen's hands at four points are given in Figure 4.)

15 K: But in the winter, the rainfall times [a] what historically might have
16 been, a [b] say [c] a [b] 2 inch [c] rainfall [c] event might have gone
17 up to about 3000 liters a second. What we're getting [d] is, we're
18 getting up here almost, almost off the graph paper, or up to 5000 liters

19 a second. That is, in a major rainfall, when all the watershed is
20 saturated, nothing else is soaking in, either off the grass cover or off
21 the pavement.

[[[[[[[[[[Insert figure 4 about here]]]]]]]]]]

For Karen, the graph does not exist in and of itself. Rather, it is mediated by the historical evolution of the watershed (lines 15-18). It is further situated with respect to other, larger watersheds and with respect to the season (winter) when such rainfall events occur contrasting (extremely) low water levels in summer when the farms need it most for irrigating their fields. Furthermore, elsewhere in the transcript Karen situates the increase from 3000 to the projected 5000 liters/second flow rate, on the one hand, relative to small and large watersheds, on the other hand. Smaller watersheds suffer from flash floods, especially with the large number of impervious surfaces and straightening of the stream that Henderson Creek and the community as a whole have experienced in the past. Finally, the graph does not just show 3000 or 5000 liters/second, but these values exist in relation to the physical characteristics of the watershed, the grass cover and pavements (lines 20-21). Karen also knows that if more than 12% of a watershed are covered by impervious surfaces (e.g., pavement), its health will be seriously affected. In this watershed, the impervious surfaces have increased tremendously over the past two decades. The mediating relation of the community and its history is further highlighted in the following excerpt.

21 K: There are about 12 licenses on the whole creek. And that was all made,
22 all these decisions were done like in the late forties based on zero
23 knowledge of this creek, this watershed. So, we finally decided well,
24 they don't have the funds, so we're just gonna pay for one. The
25 municipality has gotten their own station just down stream at Stella's
26 Road and Wally's Drive. So, they're monitoring up there for changes

27 in the fluctuations of the flow, we're monitoring down here, so we've
28 pretty much covered the whole watershed.

Here, Karen's work with graph inscribes itself in a situation that has historical roots to the 1940s. At that time, her farm as well as 11 others received their water licenses, although, as she emphatically pointed out, there was little known about the ecological complexity of watersheds, their watercourses, and the underground aquifers that feed them. Furthermore, what happens at her monitoring station is also linked to, and interacts with, what happens at other water monitoring stations. Thus, Karen's reading of the graph becomes meaningful in the ensemble of mediated relation to other currently existing practices and to the watering and communal water distribution practices from which they have evolved.⁴ Karen's activity inscribes itself in a historical context. The years she has spent as a water technician in the watershed have given her many opportunities to talk with farmers (other than her employer), First Nations people, and other local residents who have been living next to the creek for more than half a century. As a member of the environmental activist group, Karen also has access to the historical records that speak of plenty in terms of water resources (e.g., people used to canoe in the creek) and trout sizes and quantities no longer heard of.

There are farms with water licenses that take water from the creek between her own monitoring station and that placed by the community. The differences between Karen's own readings and those coming from the station of the municipality are also important to her work. The water monitoring station and the graph it churns out also exist in the context of the entire water budget of the watershed. In fact, Karen and the other technicians and engineers she collaborates with have done calculations of the total rainfall on the watershed and compared it to

⁴ Two other relations are notable in the transcript. First, Karen's reading of the graph is mediated by another graph not present in the setting. As a form of division of labor, Environment Canada technicians have determined this function and also convert the water level chart into volume charts each year. Second, Karen's hand-finger movements across the paper stand in an iconic relation to the movement of the pen. That is, Karen's reading of the graph also exists in the context of her embodied understanding of the instrument that records the graphs. Both of these relations are discussed below.

the amount of water that flows out of it at the station, which is only 300 meters from the mouth of the creek.

Karen is also familiar with the relationship between the amount of rainfall and the response by the watershed in terms of the amount of water that will be shown on her graph. Here we have, embodied in her practices, another translation and semiotic connection which contribute to Karen's competent reading.

One of the questions asked by visitors related to the minimum water flow required by the fish, "Does the water level affect temperature or oxygenation levels?" Karen first did not address either temperature or oxygenation but responded that fish needed a minimum depth for navigating the creek. Then she picked up the question of temperature and oxygenation.

29 K: Yeah certainly, as the flow gets lower the temperature would get higher.
30 Because they only got this much water to heat up, it's gonna all get
31 warm throughout it. It but if it's this deep and there's a pocket that is
32 covered into the bank you can... You gonna have a nice little hiding
33 spot. I think they need anywhere from 8 to 11 parts per million of
34 oxygen. Most fish do. We have little sticklebacks that, actually they eat
35 them. They can survive at 2 parts per million oxygen completely
36 exposed sunlight areas. So where there is a food supply, there's still no
37 cutthroat trout because they are not gonna follow them into those areas.
38 In terms of temperature, anything around 13 is a really nice temperature,
39 they will, the bigger grand daddy kind a cutthroat that hang out here. In
40 the summer, it's like 27. In this fully exposed area. But down at the
41 bottom, they've got a seven-foot depth to hang out when the dam is in.
42 And they got cool temperatures down at the bottom.

Karen is very familiar with the creek. We have walked along its bed numerous times, including other individuals interested in the restoration of Henderson Creek or consultants. Karen has constructed riffles from local rocks to improve the oxygenation rates, and planted trees that eventually would provide habitat. She has used a dissolved-oxygen meter to determine the oxygenation of the creek water both above and below the riffles she single-handedly built on the farm property, or in collaboration with the other activists in other parts of the creek.

In this excerpt, we can recognize Karen's familiarity with the creek as an ecological and a physical system. First, the water flow will affect water temperature (lines 29-31), the temperature lowers the dissolved oxygen (lines 33, 35-36), and there are temperature gradients in deep water. All of these factors affect where cutthroat trout and sticklebacks (trout food) can live during different parts of the year and especially during the summer months (lines 37-41). Thus, Karen's reading of the graph is not independent of her understanding of the creek, the physical characteristics of heat capacity, and ecological relationships between species that have different requirements on their physical environment. Karen's reading of the graph during the summer months exists in and as of the mediating relations in respect to the creek.

In the tight network constituted by these relations, Karen navigates between the different representations of the creek (i.e., signifiers that characterize knowledge about the creek) and integrates the tools and history. Yet we must not forget that this integration is achieved in and through Karen's activity. We need to remind ourselves that the different representations (signs) Karen uses in her activity are nevertheless distinct and arbitrary in the way Latour (1999) theorized the situation. As she works in the creek, her familiarity with the setting increases. Furthermore, the outcomes of her activities provide additional mediating tools for understanding the creek. For example, Karen measures the water level in the creek using the pen chart recorder connected to the measurement device. As an outcome of this activity, she gets graphs that monitor the water level throughout the year. These graphs then become new tools that mediate her relationship with the object and in fact constitute Karen as a 'more knowledgeable' subject and the creek as a 'better-known' object. This development over time is represented in Figure 5a.

The Environment Canada technician also gets into the creek, establishing cross section data, maps these against water levels, and constructs a calibration curve (lines 43-46). These curves are themselves an outcome of an activity and become mediating tools in Karen's work. Karen is familiar with major markers established by the calibration curve. In fact, when she reads the graph, she talks about water volumes rather than the water levels displayed. But she does not actually produce the water volume graphs (e.g., Figures 6) herself. This too is done by the technician from Environment Canada, and as she repeatedly emphasizes, takes about a year to get done.

49 K: It kind of takes a year after the information collected to process it and
50 for 6000 \$ cost. So, an Environment Canada technician comes down,
51 scoops the whole roll up, takes it back to his office and calculates what
52 that line means.

Nevertheless, the resultant graphs come back to the community to be used by Karen, the farmer, and the environmentalists for a variety of purposes. For example, graphs may become part of a proposal that seeks further funding so that Karen can continue her work. Figure 6a shows two graphs taken at different places in the watershed. In respect to this figure, the main body of the proposal reads:

Discharge measurements are generally 6 to 10 times greater at downstream site than at a flume site. The downstream site, a water survey station on Oceanside Farm is roughly 2 km below the flume site on the Gooding's Farm. In between these sites, 7 small tributaries feed the main creek, yet there is negligible flow in them during the summer period. The inflow is believed to be due to the influence of the nearby bedrock aquifer just to the north of the valley. Bedrock is observed to form sections of the main streambed. [From proposal to fund Karen's position.]

Nadine (the teacher) or Walter (the mayor-visitor to Open House) exists in relation to other graphs Karen, her activist colleagues and others in the community work with. The three graphs displayed here exist in and through their relation with the graph at Karen's hand, but also with respect to each other. Evidence such as that provided in this section supports the contention that Karen's graphing competence is embedded in many other mediated relations (Figure 3). I contend that these mediated relations constitute the context that makes the graphs meaningful. (This will force us to reconsider the notion of context in school mathematics.) However, Karen's competence also involves a very physical, embodied component, which is described in the following section.

Embodiment

Knowing the source of the data and the instruments by means of which data are collected was an important aspect of scientists' determining the level of competency (Roth & Bowen, in press). When scientists were unfamiliar, their readings often involved mis-readings that shared similarities with those of high school students. This is also the case for Karen. In this subsection, I show that reading graphs is an embodied activity, against the graph as a ground. Gestures are used together with language so that the three constitute a communicative ensemble that is much more complex than talk would be by itself. It is not only the text, but Nadine can see embodied in Karen's gesture an iconic representation of the pen (shaded inverse "T" next to curve in Figures 1, 4) moving across the paper, inscribing the line that is the focus of the present interaction.

Karen knows the instrument that records the water level graphs and in particular the mechanism by means of which the curve is being taken. She knows the instrument so well that her body participates in communicating the functioning of the device. Consider her presentation featured in Figure 7a. Here, Karen's hand moves from right to left along the horizontal direction of the paper while uttering "hours go this way." Her hand follows the direction of the paper in the pen chart recorder, taking the same trajectory. The gesture therefore stands in an iconic relationship with the tracking paper. Time is not just a label on the axis, but is something that

continuously unfolds and is indexed by the turning wheels and moving paper. Karen has a very embodied understanding of time as it pertains to her graphs. Interestingly enough, indicating the time through a bodily movement may depend on the circumstance, for in another situation, Karen's gesture described a trajectory in the opposite direction. Here, her gesture described the trajectory of the graph as it unfolds on the paper under the pen. Here, Karen's hands track the apparent direction of the pen across the paper. In both situations, time was something embodied in the (apparent) motion of the paper or pen, and embodied in her gesture.

[[[[[[[[[[Insert figure 7 about here]]]]]]]]]]

Karen does not just know the relationship between some sign (point on graph) and the amount of water. Her gestures embody the working of the pen. As Karen talks, her hand-finger movement (sequence Figures 4a through 4d) moves along a trajectory similar to that of the pen. The trajectory of her finger, therefore, stands in an iconic relation to that of the pen similarly to her movements portrayed in Figure 1. Interrupted by the movement and gesture that indicated the distance on the paper that amounts to one day, her finger moves, similar to the pen, across the paper. In the same way, the to-and-fro movement of the pen is embodied in her hand moving up and down along the now vertical side of the chart.

The engagement of her entire body in representing the recording in terms of sensori-motor experience is even more pronounced in the following episode. Here, Karen explains the source of the graphs to a visitor to the Open House (Walter, the mayor of Oceanside).

53 K: So, the way this works is there's pipes going across the creek and the
 54 water comes into the still(ing?) well area and this is, the fluctuations in
 55 that water level drive this wheel here and then this pen works.

As Karen talks about the well in which the water fluctuations drive a floater, her arms form a circle, she bends her knees, so that, as a whole, she describes a drum-like object. Right after, Karen enacts the graph recording with her entire body, hand and body standing for (i.e.,

representing) the pen and floating device, respectively (Figure 7b). She begins to bend her knees so that her body moves downward like a piston “inside the equipment” in “the upright column,” while her right hand follows in and amplifies the downward and upward movement of her body. But in this, Karen’s sensori-motor actions are not just indexical to the floater, but to the fluctuations of the water level (the object in Figure 3) throughout the year (see utterances in Figure 7b). Karen performs the recording, her right hand embodying the pen movement, then her entire body enacting the up and down of the floater in the stilling well, her right hand an iconic relation to the recording device.

In these examples, we see Karen not just talk about but move (parts of) her body through trajectories that stand in iconic relations to the graph, paper, or recording device. The movements of these entities, which she observed frequently over the past four years, exist as sensori-motor representations in Karen’s experience, and are available in public to her listeners. The movements of pen and paper, which exist in the material trace of the graph, are literally embodied. The meaning of “time goes this way” and Karen’s up and down movement with her body, followed by her hand is simultaneously built on two types of meanings. First, it built on the sensori-motor action involving Karen’s finger (hand) over (in front of) the plotting paper and the graphical space it defines. Second, Karen draws on the symbolic meanings associated with the marks and lines on the paper of the conventional graphical signs. It has been pointed out that for physicists, indexical gestures, taken as sensori-motor and symbolic re-enactments of material events, are an integral part of the discourse practices through which physicists come to their understandings (Ochs, Gonzales, & Jacoby, 1996). The sensori-motor processes therefore constitute an important aspect of collective processes of meaning making, and the witnessing of the Other’s subjective understandings. The graphs thereby constitute subjects and objects in referential ways as simultaneous, co-existing participants in the described events (Ochs et al., 1996).

Sociologists and philosophers, and more recently artificial intelligence and cognitive scientists view learning as the structuring of mind, which is fashioned during bodily interactions

with the social and material world (e.g., Bourdieu, 1997; Merleau-Ponty, 1945). Linguistic studies suggest that our language is deeply grounded in and arises from the mid-level (not too tall, not too small) entities that we encounter in the world (e.g., Lakoff, 1987; Roth, 1999). Here, my recordings of Karen constitute an exemplary case. Here understanding of the graphs is deeply linked to her understanding of the water level recording device.

To summarize, Karen's graphing competencies have a strong physical component, which I exemplified here in terms of the relation between her gestures, the recording device, and the graph. However, other physical relations also exist, for Karen's understanding of the creek is tied to her in-creek activities, building riffles, catching trout, planting trees, etc.

Graphs in Face-to-Face Interactions

Before discussing the relevance of this work to mathematical cognition and development, I want to point out an important aspect of graphing as it has arisen from my work. Until now, my description focused largely on different relations involving Karen and other aspects of the setting. However, I have not yet addressed the role and importance of graphs in face-to-face interactions. Here, graphs can become sites where social interactions occur over issues that are relevant to the lives of the people living in the area. One reason for the low frequency of face-to-face interactions is the type of situations in which Karen was recorded. Both with the teachers on the farm and with the visitors to the Open House, Karen explained the graphs and her work. She was in what we might term a knowledge display mode. However, there are many instances in my transcripts with interactions beyond continuers. (In conversation analysis, 'continuers' are turns that allow the current speaker to continue speaking, such as 'Yes,' 'OK,' or 'Is that right'.) She has prepared her exhibit at the Open House of the environmental activist group. She intended to show and explain to people what her work consists of, and how it inscribes itself in the life of the community, and in the plans that the activists have for improving the water quality and quantity.

As she is in display mode, and these are her graphs, Karen talks. However, when a graph is a public object, there is always the potential that other persons will contribute their readings. In this case, a visitor to the open house (Walter, the Mayor of Oceanside and principal of local

middle school) does not just let her continue, but contributes in an active way. He talks while Karen is still going, making a bit to talk. (Karen’s deictic gesture is depicted in Figure 8.) Walter injects his hypothesis based on his own reading of the graph. As a consequence, the episode does not just constitute mere display, and is not only about the graph. Rather, the episode is an exchange that takes the graph as its starting point and elaborates many issues related to it.

- 56 K: GESTURE[Figure 8] And then there is superimposed rainfall up there
 57 and [one of these
 58 W: [Does it say?
 59 K: Pardon?
 60 W: Does it say, ‘Now I know when that will peak?’
 61 K: Aha, good. So, one of these little squares is 2 millimeters.

[[[[[[[[[[Insert figure 8 about here]]]]]]]]]]

Karen did not expect Walter’s interjection but her “Pardon?” requests a restatement. Walter therefore obtains a turn in which he elaborates his *passing theory* (Rorty, 1989) about the topic at hand. Karen then acknowledges his theory, but continues with an explanation of the conventions (scale) rather than addressing the relation of the rainfall with the peak of the water level.

Presenting her work in public, Karen navigates the tension between interacting with the audience and presenting the other with what she might consider to be the foundational knowledge required for being able to read the graph. Yet, there is always a tension involved in such relations (e.g., Walkerdine, 1988). Here it is one of who owns the interpretation of the graph, and therefore the speaking platform. But there is an additional tension arising from the fact that the conversational topic can be shifted to be about something else, here the entire valley and its water resources. Karen began in display mode, and continuous in her attempt to retain the position as a presenter rather than engaging in a fully open interaction. This changes when the topic moves to consider the watershed itself rather than the sign that mediates the knowledge

about it (at least in as far as Henderson Creek is concerned). A few minutes after the above exchange, Walter indicates that he also lives in the valley and that he has one of the water licenses. Subsequently, the interactions between the Karen and Walter appear to change in kind. They begin to talk not just about the graph, but about the issues for which the graph stands in a reflexive relation to the water, valley, history of settlement, and changes in farming. At this point, both own the issues, and thereby construct each other as equal contributors.

The following episode begins when Karen talks about irrigation and vertical jumps in the graph that stand in a reflexive relationship with irrigation practices.

62 K: These very, you know, 90° angles in the lines, that's definitely straight,
63 straight drops. That's definitely irrigation that decreases, people are all
64 stopping at the same time, starting at the same time. And the conditions,
65 it's dry for a while here. GESTURE[as in Figure 8].

66 W: Yeah, a lot of hay, people are into the hay.

67 K: Yeah, a lot of people cut it at the same time.

68 W: Further, you go towards the Fellow's farm. Down Henderson Creek.

69 Because once you get past Fellow's, it stops. There is corn. But of
70 course, nowadays, there is late corn, too.

71 K: Yeah, they grow different varieties.

72 W: I think they grow mostly early corn on the fields that are around
73 Henderson Creek.

74 K: Corn has a lot, requires lots of water, doesn't it? Compared to hay.

In this episode, Karen introduces the topic of irrigation, which goes with particular vertical discontinuities (jumps) in the graph. But it is not just that these jumps are signs that stand in a signifying relation to the water level changes caused by irrigation. Rather, irrigation also stands in relation to the second, layered graphical information on the top border of the graph (Figure 8).

Presently, Karen and Walter stand in front of that part of the roll that was recorded during the summer. There are no rainfall events marked on the top part of the paper roll. Thus, the jumps attributed in this episode to irrigation exist in relation to the time of recording (summer), the number and size of the (here lacking) rainfall events. Most importantly, the topic in the episode is not some feature of the graph, but the farming practices and irrigation that obtain in the valley at the present time. Yet all this is part of the thick layer of knowledge and experience that brings forth the extraordinary competence in the first place. Here, and as a 17-year inhabitant of the valley, Walter is a knowledgeable conversation participant. He is as familiar as Karen with the hay farming that goes on in the summer, which requires the dry conditions of (late) summer in this part of the world. Karen then suggests that many farmers begin and stop irrigation at about the same time, a fact again related to the weather patterns in the valley and haying practices that require a dry period for each harvest.

Walter subsequently adds that not all of the farms grow hay, but that they also grow (different types of) corn. He even provides a description of the specific farm where the corn crops begin to dominate the fields (line 68-70). Karen then makes a statement—which can be heard as a question to Walter who had previously already talked considerably about strawberry farming practices—that corn takes more water to grow than hay. This, in turn, would have significant impact on the irrigation practices (especially if there are different types of corn) with a resultant effect on the water levels and Karen's charts.

This episode shows that graphs are not just signs standing in a unique and unambiguous relationship to objects. Furthermore, they are not just objects of knowledge in the way that past developmental research in mathematics treated them. Rather, as in the previous analyses, the primary object of the interaction between Walter and Karen is the creek and the surrounding valley in which it is located. The graph is but an object that anchors the social space in which the two collectively engage in the construction of the watershed for the purposes at hand.

To Know Graphs

In the foregoing sections, I showed different aspects of knowing graphs. These different episodes show that mathematics in everyday practice is constituted in a noisy field of practical action and discursive relations. In this practice, graphs do not exist as ideal Platonic objects with definite structure and elements. Rather, in the context of particular practices, graphs make available what is necessary in the situation at hand. Other structural aspects that a theorist may identify remain undisclosed. (For example, Karen needs neither to read individual data values nor to identify the slopes of the graphs.) What matters in the context of her work are those differences that make a difference; that is, differences that contribute to the relations that constitute the heuristic entities in the mediational triangle (e.g., subject, object, tools, and division of labor). Thus, it matters in the Karen-creek-graph relation that a particular graphical feature arises from a clogged pipe in the instrument or the lifting of a dam rather than some other event in the watershed.

The graphs do not just serve to express something about nature (in this instance the watershed). Rather there are very different, economic and personal matters in which these graphs are inscribed. Here, the proposal from which the three graphs in Figure 6 were culled was seemingly written to seek funding for monitoring the water budget in the watershed. But at another level, the technician to be employed with the funding received is Karen herself. The graph that Karen reads to different audiences is not just a representation, it is lived as a relation within a range of practices and her life of being a water technician. This graph exists in relation to the ending contract that provides for her subsistence and a new contract with the prospects of continuing her work at a place that she has come to be very familiar with.

“Context” has been one of the focal points in the discussion of how to make mathematics more relevant. In a recent article, I asked the question “Where is the context in contextual word problems?” (Roth, 1996). The present chapter contributes answers, from my perspective, in new ways. It is evident that situated cognition does not mean that people think differently in different contexts (Walkerdine, 1997). For the signifiers may be the same, but because of the different

relations that they mediate, they in fact contribute to constituting the context in different ways. In everyday practice, such as that Karen enacts, the many different relations (e.g., Figures 5) contribute to an over-determination of any individual relation and the objects and tools involved. At the same time, unlike former assumptions concerned only with the relation between sign and world (Figure 2a) or sign, world, and interpretant community (Figure 2b), the change in objects and tools also changes the way in which subjects are constituted. Thus, Karen's subjectivity changes over time (Figure 5a), through interactions related to division of labor (Figure 5b), and in individual interactions. Thus, Karen is constructed differently as a subject in her interaction with Nadine (expert) than with Walter who, along a number of dimensions, is more familiar with and knowledgeable about the valley, community, creek, farming practices, or watershed. Without considering the relations, we would draw inappropriate inferences about the nature and extent of someone's knowledge based on analyses of the data we have at hand.

From a phenomenological point of view, what imports is the lifeworld, the world perceived and acted in by the person-in-activity. Activity theorists argue that the concrete embeddedness and meaning of activity cannot be accounted for by analysis of the immediate situation. They assume that all concrete social institutions and relations are characterized by historically emerging contradictions (Lave, 1993). But they emphasize, at the same time, that objectively existing social structures do not have a determinate effect. Any meaning is socially constituted in relations between activity systems and persons acting in the world. Meaning always has a relational character.

The point I am making is that it does not bring us much further if we view context as a container that can be grafted intact onto cognition or cognitive development. The social is more than a container of the psychological, but each of the two arises from complex dynamics by means of which they are constituted in actual practice. Furthermore, signs are produced and used within the dynamic intersection of actions, objects, and speech within a practice and therefore function as relations within the practice. Signification, therefore, cannot be reduced to representation (Walkerdine, 1988). Walkerdine concludes that participants themselves therefore

become in and through the relations in which they are embedded. Karen is who she is in relation to her employer-farmer, the water conservation and creek restoration efforts of her activist group, and Nadine who has sought her as a consultant for a school-related project. “Karen” also emerges from the relations with the First Nations people, the creek that she so intimately knows, and the Mayor, Walter, who participate in the reading of graphs in relation to the community.

In the episodes featured earlier, Karen navigates the ontological gap that exists between (features of) the graph and those features of the Henderson Creek watershed with which it stands in an indexical and reflexive relationship. For example, when she talked with Walter about the irrigation, neither individual seemed to have a problem talking about the vertical jumps in the graph in terms of the irrigation. In fact, the conversation shifted and was concerned with the object, Henderson Creek (watershed), the knowledge about which is mediated by the graph. That is, in praxis, the ontological gaps do not appear to exist. In Karen’s work and interactions with others, the graph seems to be transparent, providing her with a window on the world of the watershed. At this point, a troublesome question demands attention. How did Karen get there? This question has to be central to the activities of mathematics educators, for if, as I pointed out earlier, there are ontological gaps between representations, how do individuals ever come to the point of using graphs as if these gaps did not exist?

Implications for Learning and Development

Heeding the Ontological Gap

Past research on graphing made (sometimes implicitly, sometimes explicitly) use of a theoretical frame in which the relationship between graphs (as sign, symbol) have an implicit relationship to the world or some other sign. Thus, in the research on graphing, investigators asked students to interpret a graph or select among graphs the one that referred to some situation (e.g., Leinhardt et al., 1990). These students were frequently untutored (not instructed) in graph use, and had few opportunities to engage in representation practices.

In one typical task, students are asked to walk across the room and return to their starting point. They are then asked questions about graphs or asked to select that graph which best represented their trip across the room in terms of distance or position and velocity (e.g., Berg & Smith, 1994). Not surprisingly, large numbers of students answered inappropriately or selected graphs that were inconsistent with scientific practices. Kaput (1988) and Greeno (1988) discuss the use of a winch as a pedagogical device to allow students first-hand experience with a phenomenon that can be modeled mathematically by using linear functions (height = $f[\text{turns}]$). In the past, some mathematics teachers (as science educators) have assumed that mere exposure to such (hands-on) activities is sufficient for learning mathematics (science). Of course, this assumption is justified if we assume that there exists an isomorphism between the world (here the winch) and mathematics. Counting turns and measuring the length of string wound onto the winch share deep structure; measuring length can be reduced to counting equidistant intervals. However, turning and getting a bucket of water from a deep well are not inherently mathematical. If this assumption does not hold, as in my framework, we have little reason to expect that students infer mathematical knowledge from interacting with the device. What traditional educators forget is that our network of (discursive, mathematical, and material) practices is so extended and so habitual that we no longer remark the ontological gaps that separate them.

A central assumption in cognitive research on mathematics is that structures are *inherent* across contexts. Thus, any linear function would be constant if it involved turning the crank of a stilling well to bring up the water bucket a certain way, increasing the velocity of a ball as it rolls down an incline, or increasing the height of a stack by adding books all. What we need however is to examine these relations as relations of signification. It becomes evident, then, that each practice is different though relations between them can be specified. In this case, “situated cognition is not people thinking in different contexts, but subjects produced differently in different practices” (Walkerdine, 1992, p. 15). Certain transformations are therefore necessary to turn non-school practices into school mathematics practices.

When we take a traditional perspective and assume logical relations to exist between different sign systems, or even within sign systems, we would come to the conclusion that these students were not able to derive the relationship between walk and graph. That is, these students lacked the skill or capacity for making logical inferences. They were said to be stricken with cognitive deficiencies, mental deficits, misconceptions, and so on. It is easy to understand such conclusions, because they derive from sign-referent relationships that are given a priori. We come to entirely different conclusions if we take a sociomaterial-practice perspective on ordering and representing activities. There are, therefore, no inherent logical grounds, but merely negotiated and shared ways of engaging in particular activities. From such a perspective, we would not expect individuals to derive the relation between two representations or between worldly events (walking across the room, turning a winch) and some mathematical representation. Rather, we would ask questions about the extent to which these individuals have participated in the practices. If there had been little prior participation, we would expect to see little resemblance between established practices and the activities that the individuals engaged in. It is not surprising, then, especially within the psychological frame applied, that this research focused on the deficiencies people bring to the task of relating signs and aspects of the world.

From Inside to Outside

Graphs are social objects in at least two senses. First, graphs only exist and have meaning in relation to the place they have in some social practice. They are used in such places as poster displays, scientific articles, newspapers, or books. Here, readers who have previously participated in reading and graphing practices disclose through the process of their reading what the author intended the graphs to communicate. As such, graphs only exist in and as of their relation to sign-related practices. Second, graphs can become the site of face-to-face interactions between people who negotiate, in real time, what graphs are meant to express, how they inscribe themselves in the issues at hand, and so forth. Important understandings of graphing practices arose in the context of a micro-analytic study of mathematical representation practices in a grade 8 classroom where students transformed nature into different sign forms, and interpreted the sign

forms created by their peers (Roth, 1996). It turned out that these students developed considerable competence in transforming the material-form elements from Figure 1c in both directions. On the one hand, they developed increasing competence in using graphs and statistics as a way to construct and express understandings about 35-m² plots of nature. On the other hand, they equally developed a tremendous competence in interpreting existing representations, that is, to create verbal descriptions of natural situations that could have been the origin of the graph. We conducted a quantitative study to compare their competencies to those of college science graduates enrolled in a fifth-year teacher education program. The task was based on pairs of numbers (light intensity, plant density) that were entered in each section of a subdivided plot of land; participants were asked whether there was a relationship between the two measures and how they could support their answers. There was a statistically higher use of graphs and statistics in the grade 8 responses than among those by the college graduates (Roth, McGinn, & Bowen, 1998). Our interpretation, consistent with our theoretical framework, did not use deficiency as an explanatory resource. Rather, we argued that the grade 8 students were much more familiar and had more opportunities to enact the representation practices.

We began our research on graphing in science classrooms assuming that scientists were experts that we could use to constitute a normative frame for expertise. Our interviews with 16 scientists (mostly ecologists) taught us to rethink our assumptions, for there were many instances when scientists did not provide the kind of expert interpretations. Rather, although the graphs were culled from undergraduate textbooks in their own domain, ecologists often read graphs in ways that mathematics research has come to denote with 'iconic errors,' 'slope-height confusions,' and more generally, with 'misconceptions' (e.g., Roth & Bowen, 1999d). Furthermore, rather than engaging in an inductive process where the referent of a graph was unfoldingly disclosed, we observed a dialectic process in which ecologists played their knowledge of known ecological systems against tentative readings of the graph. Their interpretation arose as a result of a dialectically constituted reading of graphs. At the same time, we found profound differences in the graph reading activities when scientists talked about graphs

that arose from their own work. Here, they began by providing minute details of the local situations they had investigated, instruments they had used, and transformation that their data were subjected to. In these accounts, the graphs were transparent means, placeholders for an extended experience in the field and laboratory. That is, even scientists did not transfer skills from one domain of graphing to another; transfer of cognitive and linguistic operations across contexts is not as frequent as research would lead us to believe (e.g., Lave, 1988; Walkerdine, 1988).

From my (sociomaterial) practice perspective, ‘individual’ cognitive development is deeply bound up with changes of participation in sociomaterial practices of a culture. Schools are primary institutions for bringing about and fostering the enculturation into practices. Past (psychological) conceptions of graphing have led to misconceptions of what students should know and be able to do at particular points during their schooling. This misconception has led to ill-conceived pedagogical practices. If there is an ontological gap, relations between two domains cannot be derived on logical grounds. These relations are grounded in and given by the practices enacted by competent individuals. We need to keep in mind that out-of-school mathematical practices are inherently different from in-school practices because of the differences in the products of the practices, the relations of signification, the regulation of practices, the positioning of subjects, and the emotional investment (Walkerdine, 1992). A number of researchers on everyday mathematics point out that calculations within shopping and other practices exist in a different way than in school, but the calculations are often not the point of the activity (e.g., Lave, 1988; Scribner, 1986). This leads to a new fusion of signifier and signified.

Everyday Mathematics, Inside

In relation to schooling, it is often assumed that students can learn practices independent of the settings in which they are used. The notion of ‘authentic mathematics’ has been in circulation for some time. However, this notion makes little sense if we regard what Karen does as authentic mathematics (at least in relation to graphs). Let us assume that some teacher introduces the graphs Karen works with in order to make her classes more “authentic” or more “contextual.”

We can already say that she would never be able to bring children anywhere near to what Karen represents, for most of the relations present in Karen's activity will not be present in that of the children. What school children do seldom has a relation to other practices as we have seen in Karen's case. One alternative to traditional teaching is to expand the range of activities and related practices that provide longer chains and denser networks of signifying practices.

Graphing would then still be a school-related practice, but no longer stand on its own, but exist in relation to many other practices (material, signifying). The implication of my work is that out-of-school mathematics cannot become in-school mathematics because the kind of relations instantiated outside are so dissimilar from that instantiated inside schools. However, the best we can do is provide rich contexts in which activity structures are set into motion that allow new sets of (desirable) relations not-yet existing in the schools. Studies in my own research group (e.g., Roth, 1996) and those of others (e.g., Cobb, 1999) provide images of classrooms where such complex environments allowing multiple relations and multiple ways of constructing relations of subject to other aspects of the mediating triangle. The real trick, as Lave (1992) outlines, is not one of finding everyday problems that bear some correspondence to school problems, but in finding problems that are truly problematic to children. In more recent work (e.g., Roth & Lee, 1999), we have students in science classes create (mathematical) representations to function within the community at large. Now, there are new relations, including those between community, division of labor (between the grade 7 children and environmental activists), and children in terms of representing Henderson Creek.

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Captions

Figure 1. Karen, the water technician, reads the graph to Nadine, the practicum teacher. The graph is ‘in-the-making,’ still on the pen chart plotter in the monitoring station at the farm where Karen works.

Figure 2.a. Different views on the relationship between sign and the world. World and sign have long been considered to be separate domains, which were linked by correspondences, referential functions. b. The relationship between a sign and its referent is elaborated by another relationship of the original sign with another sign, said to be its interpretant. Because there are potentially many interpretants, semioticians speak of an infinite process of interpretation, or

infinite semiosis. c. A potentially infinite chain of signification relates world to language (Latour 1999). Each element is at the same time a sign for the previous element, and the referent for the subsequent element. Between elements, there is an ontological gap. Within each element, material can be given form. These gaps are navigated by means of shared social (representing) practices, which establish and control the relations.

Figure 3. The activity-theoretic triangle constitutes the basic unit of analysis in the present study. It shows the kind of mediations that exist between the elements isolated for heuristic purposes. Schools and research often only focus on the ‘primary’ relation between subject, object (water level in Henderson Creek), and mediating artifact (graph).

Figure 4. Karen explains where the graph would be given a major rainfall both today (d) and sometime in the past (a, c). As her finger moves back and forth on the page, it embodies the movement of the pen in response to the changing water levels.

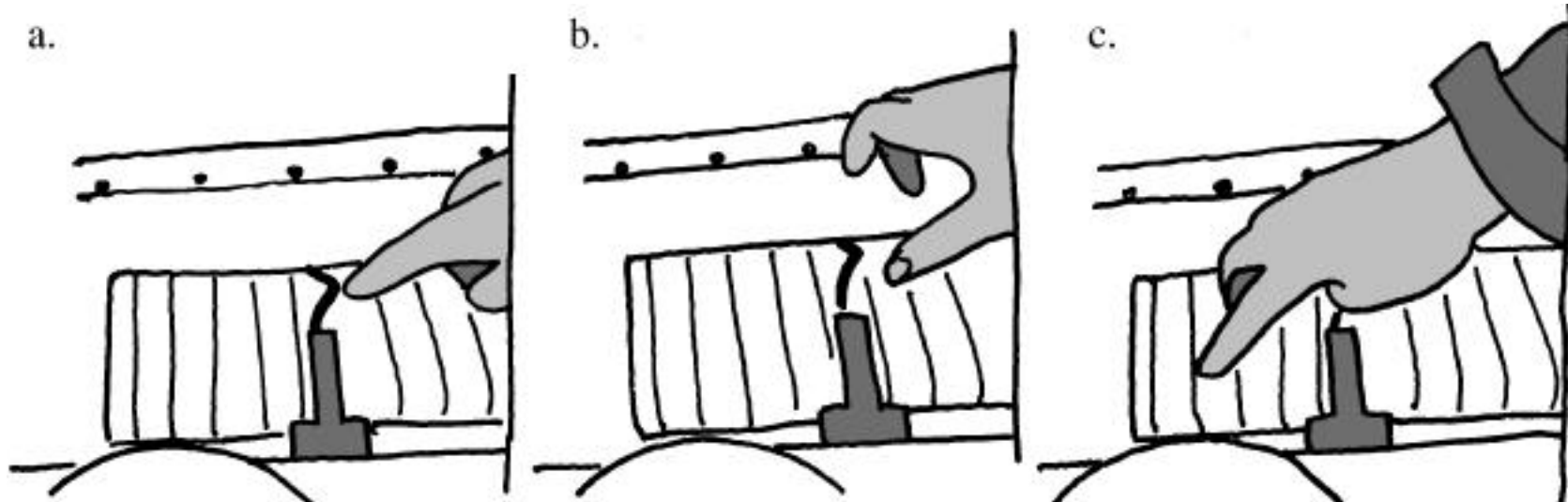
Figure 5. Changes in the mediational relations. a. Karen uses the tools at her hand to produce graphs, outcomes of her activity at some point in time. These graphs increase the number and range of mediational tools thereby constituting subject and object in and through new forms of relations. b. As an aspect of the division of labor, the Environment Canada technician uses her tools to produce a calibration curve for water levels water volume conversions. This curve becomes one of the tools appropriated by and available to Karen, mediating her own relation to creek and the water level (qua object).

Figure 6. Other artifacts mediate the understanding Karen has of the original graph. a. The water volume graph constitutes a translation and was produced by another technician using a calibration curve. b. A further translation produces a monthly discharge graph. c. Changes in ground water levels parallel the seasonal changes in discharge levels [b]; ground water accounts for the differences in two other graphs [a]. All graphs were culled from a proposal in which the activists sought funding to support Karen.

Figure 7. The gestures of Karen embody the movement of pen and paper, and the dynamics of the recording device. a. The hand shows ‘time’ as elapsing in the direction in which the paper

moves in the recording device. b. The hand embodies the pen tracking across the paper while the body moves up and down in the way the floating body in the stilling well that ultimately drives the pen.

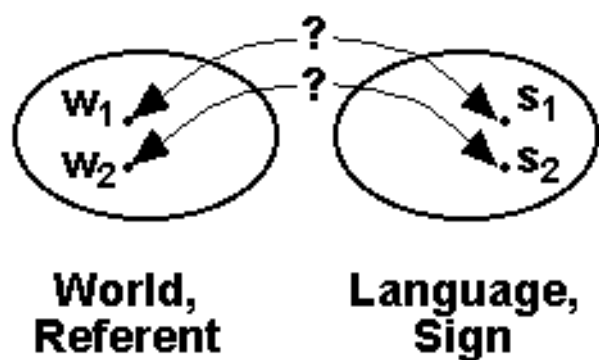
Figure 8. Karen points to a second inscription layered onto her graphs. These inscriptions signify the amount of rainfall. As she begins her explanation, Walter interjects his own hypothesis as to an inference that can be drawn about the relation between the two inscriptions.



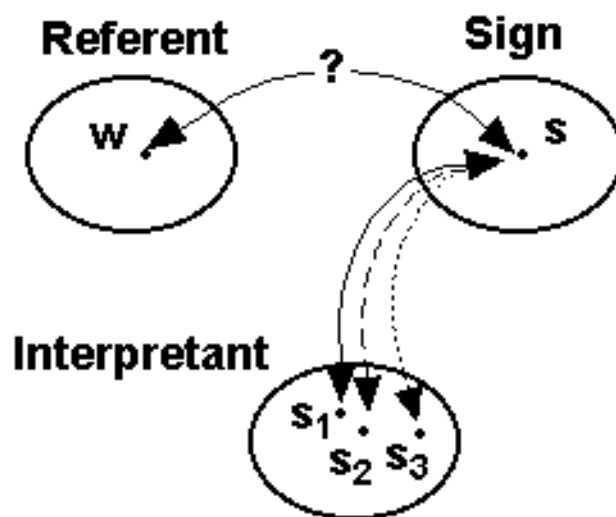
So, this [b] is a 24 hour time period, so time's going this way on the graph, so a day ago [a] the flow was about 50 liters a second higher and each square going this way is about [b] 13 liters a second. So, we were kind of, I guess we had a bit of rain yesterday [a] or the day before, and we've got a bit of a peak from that rainfall event [a]. In the summer, [c] the flow goes down to about here.

Figure 1

a.



b.



c.

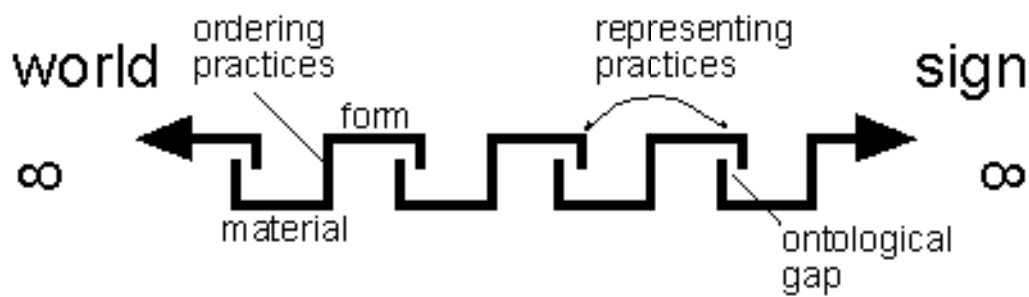


Figure 2

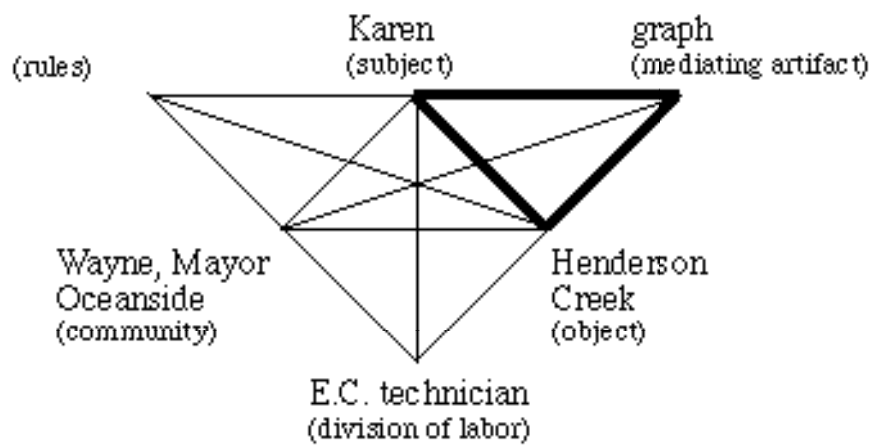
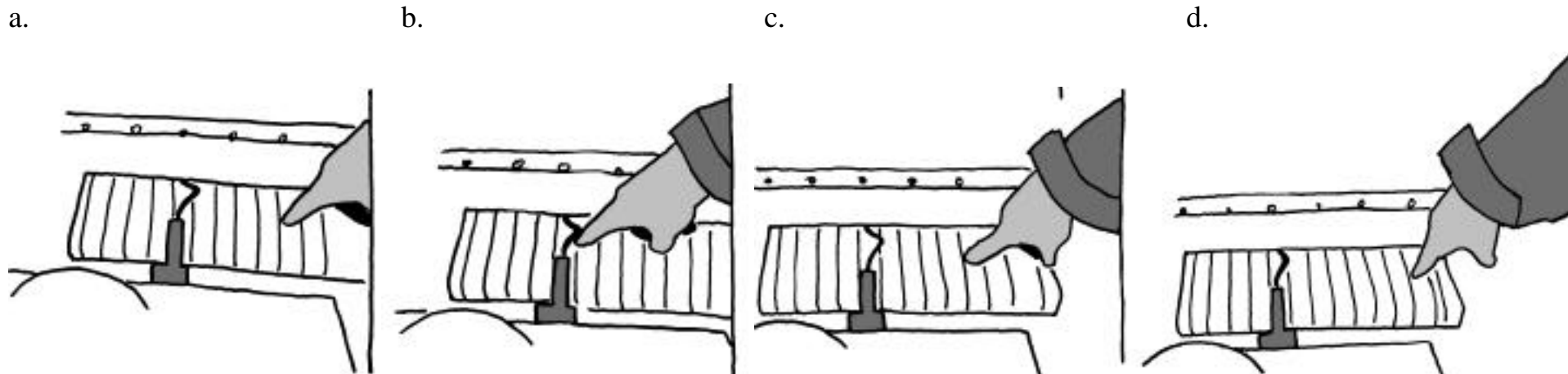


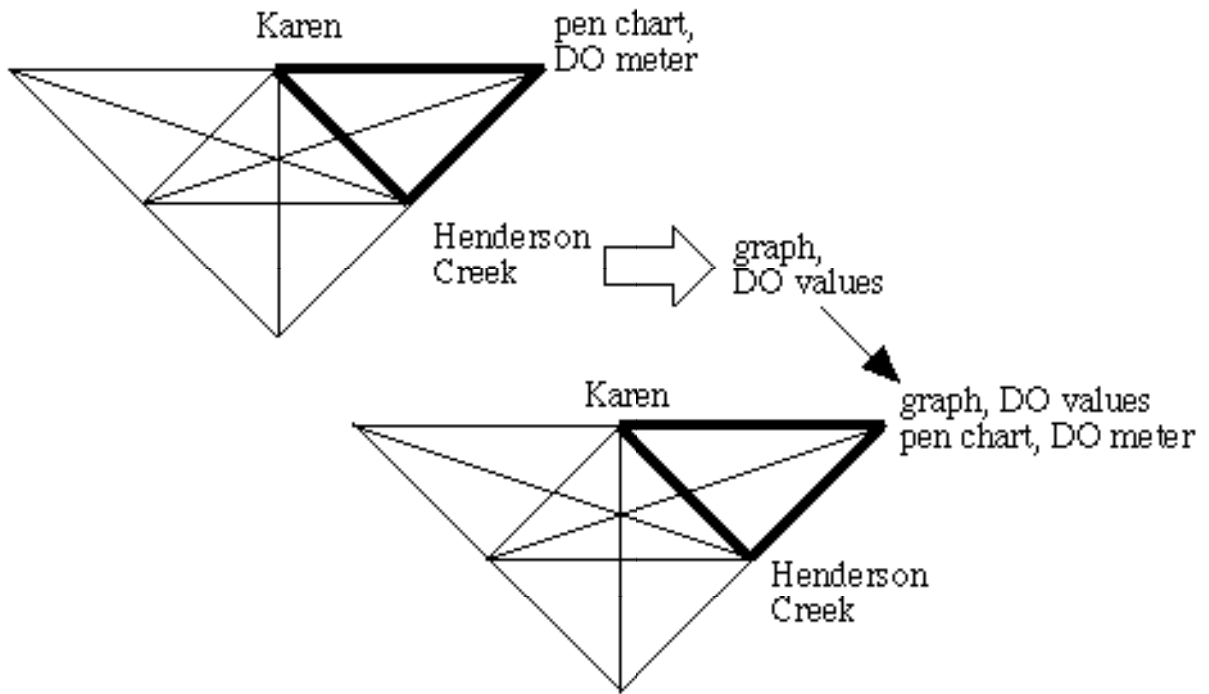
Figure 3



But in the winter, the rainfall times [a] what historically might have been, a [b] say [c] a [b] 2 inch [c] rainfall [c] event might have gone up to about 3000 liters a second. What we're getting [d] is, we're getting up to here almost, almost off the graph paper, or up to 5000 liters a second.

Figure 4

a.



b.

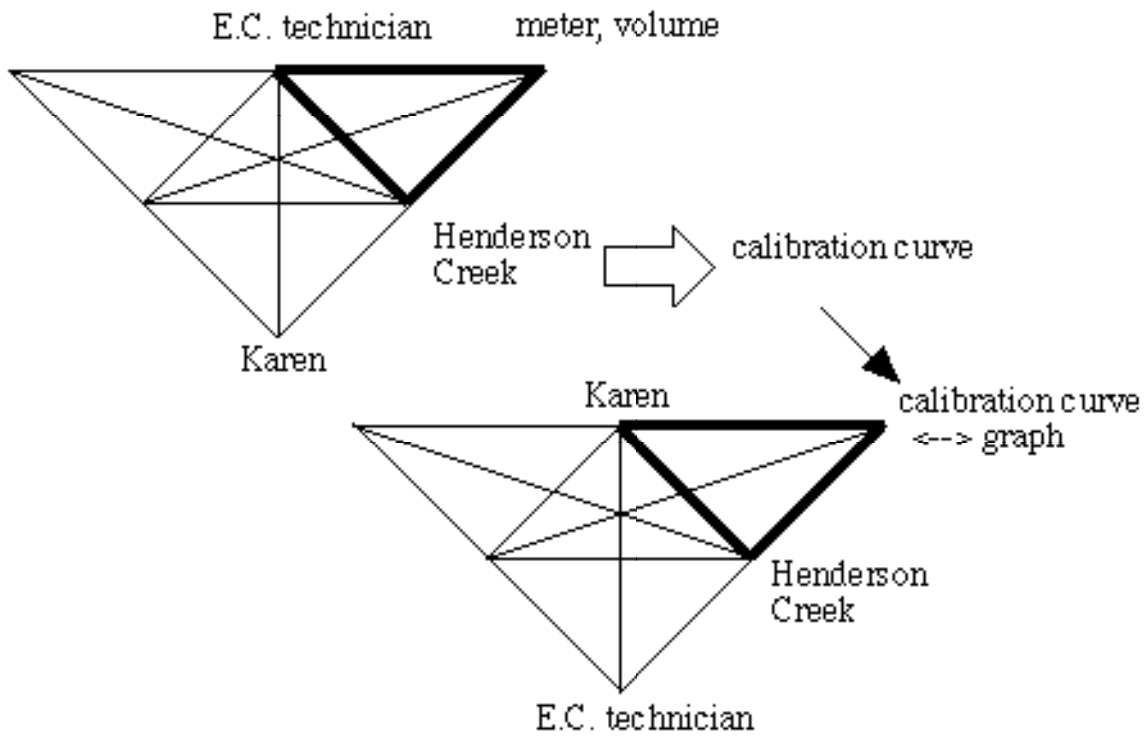
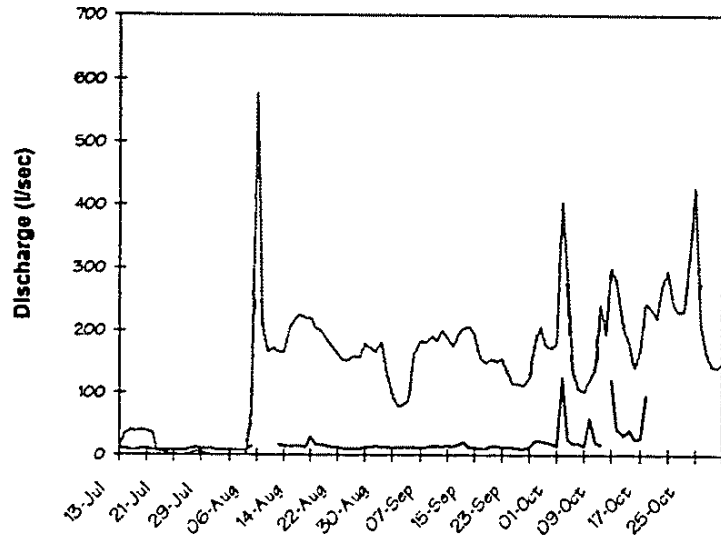
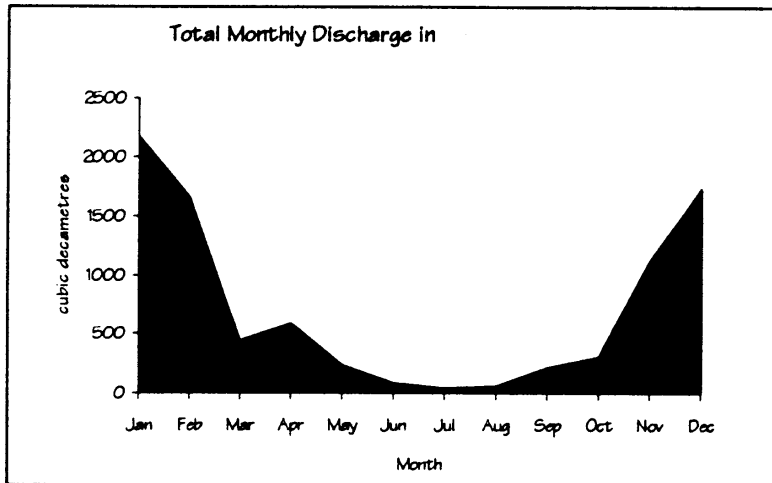


Figure 5

a.



b.



C.

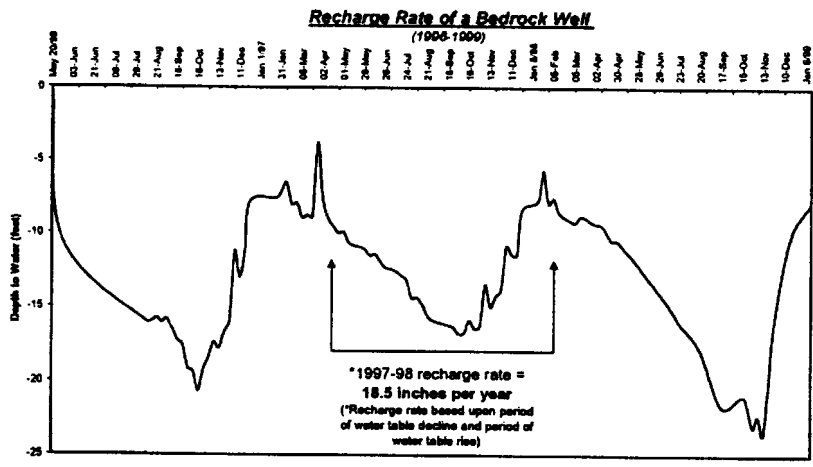
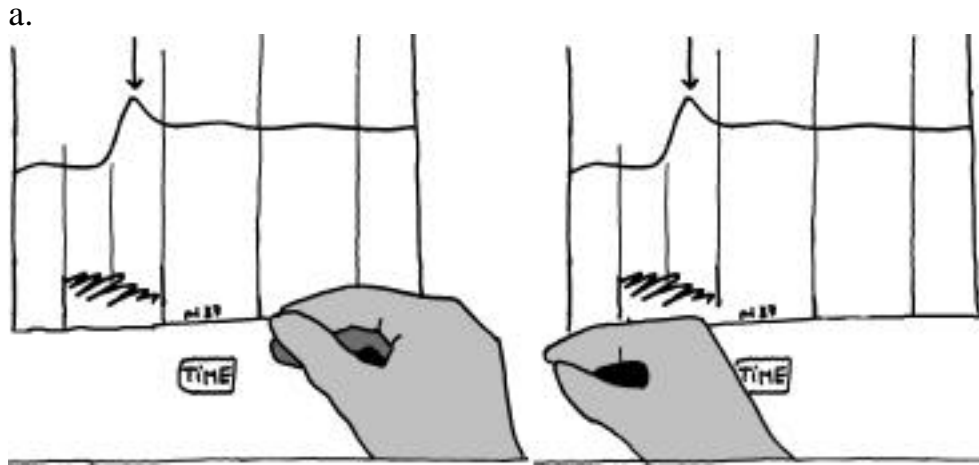
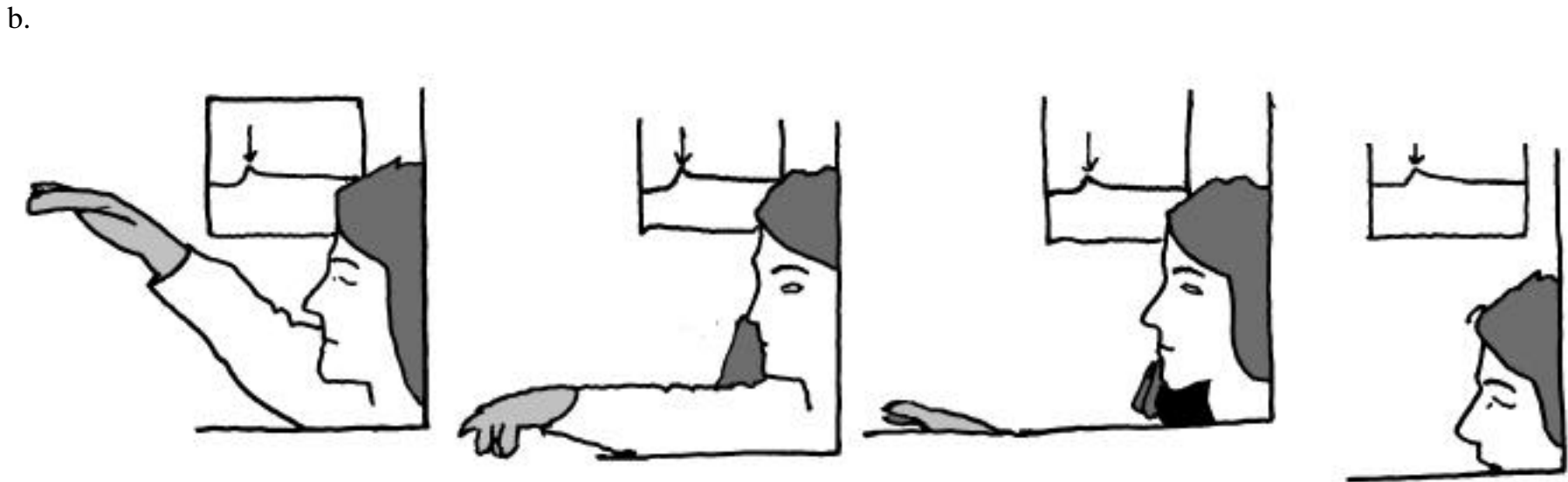


Figure 6



Hours go this way.



This is inside the equipment, the upright column... And it is fluctuating between 1.1 meter and lately, at the end of the graph, 2.1 meters.

Figure 7

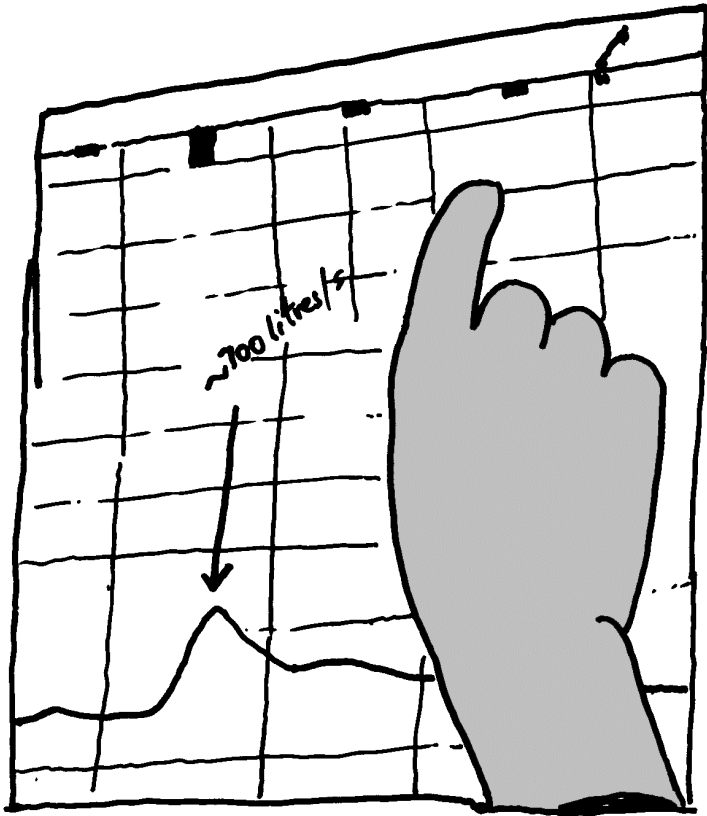


Figure 8